

## Problems on Event Generator Physics

Use the event generator of your choice for the following exercises.

1. Generate hadronic  $Z^0$  decays via  $e^+e^- \rightarrow Z^0 \rightarrow q\bar{q}$  ( $q = d, u, s, c, b$ ). Compare the charged multiplicity distribution and the distribution of  $\ln(1/x_p)$  ( $x_p = 2|\mathbf{p}|/\sqrt{s}$ ) with LEP1 data.
2. Generate  $e^+e^- \rightarrow q\bar{q}$  ( $q = d, u, s, c, b$ ) at higher energies,  $\sqrt{s} = 200, 500, 1000$  GeV. (Turn off QED radiation, otherwise you will be dominated by  $e^+e^- \rightarrow Z^0\gamma$ .)

- (a) Compare the mean charged multiplicity with the QCD prediction

$$\langle n_{\text{ch}} \rangle \sim a \frac{\exp \sqrt{cL}}{\sqrt{L}}$$

where  $a$  is a non-perturbative constant,  $c = 72/23$  and  $L = \ln(s/\Lambda^2)$ . At each energy, compute the variance and hence the error in your MC result.

- (b) Compare the position  $\xi_p$  of the peak in the distribution of  $\ln(1/x_p)$  with the QCD prediction

$$\xi_p \sim \text{const} + \frac{1}{4} \ln s .$$

3. Generate  $e^+e^- \rightarrow t\bar{t}$  at threshold and force the tops to decay leptonically (to  $e$  or  $\mu$ ).
  - (a) Compare the charged and neutral lepton  $p_T$  distributions with those shown in the lectures.
  - (b) Explain why the neutrinos tend to have higher  $p_T$  than the charged leptons. How would things change if the decay went via  $t \rightarrow bH^+$  with  $m_{H^+} = m_W$ ?
4. Same as qu.3, but for  $pp \rightarrow t\bar{t}X$  at LHC energy ( $\sqrt{s} = 14$  TeV). Here  $p_T$  should be defined relative to the direction of motion of the parent  $t$  or  $\bar{t}$ .